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### Semester One Examination, 2020

### Question/Answer booklet

# MATHEMATICS METHODS

**UNIT 1**

## Section One:

## Calculator-free

Your Name \_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_

Your Teacher’s Name \_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_

## Time allowed for this section

Reading time before commencing work: five minutes

Working time: fifty minutes

## Materials required/recommended for this section

***To be provided by the supervisor***

This Question/Answer booklet

Formula sheet

***To be provided by the candidate***

Standard items: pens (blue/black preferred), pencils (including coloured), sharpener, correction fluid/tape, eraser, ruler, highlighters

Special items: nil

## Important note to candidates

No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised material. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

|  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- |
| Question | Marks | Max | Question | Marks | Max |
| 1 |  | 8 | 6 |  | 6 |
| 2 |  | 8 | 7 |  | 5 |
| 3 |  | 6 | 8 |  | 5 |
| 4 |  | 7 |  |  |  |
| 5 |  | 5 |  |  |  |

**Structure of this paper**

|  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- |
| Section | Number of questions available | Number of questions to be answered | Working time (minutes) | Marks available | Percentage of examination |
| Section One:Calculator-free | 8 | 8 | 50 | 50 | 33 |
| Section Two:Calculator-assumed | 13 | 13 | 100 | 100 | 67 |
|  |  |  |  | **Total** | 100 |

**Instructions to candidates**

1. The rules for the conduct of the Western Australian Certificate of Education ATAR course examinations are detailed in the *Year 12 Information Handbook 2020*. Sitting this examination implies that you agree to abide by these rules.
2. Write your answers in this Question/Answer booklet.
3. You must be careful to confine your answers to the specific questions asked and to follow any instructions that are specific to a particular question.
4. Additional pages for the use of planning your answer to a question or continuing your answer to a question have been provided at the end of this Question/Answer booklet. If you use the space to continue an answer, indicate in the original answer space where the answer is continued, i.e. give the page number.
5. **Show all your working clearly.**Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
6. It is recommended that you **do not use pencil**, except in diagrams.
7. The Formula sheet is **not** to be handed in with your Question/Answer booklet.

**See Next Page**

**Section One: Calculator-free (50 Marks)**

This section has **eight (8)** questions. Answer **all** questions. Write your answers in the spaces provided.

Spare pages are included at the end of this booklet. They can be used for planning your responses and/or as additional space if required to continue an answer.

● Planning: If you use the spare pages for planning, indicate this clearly at the top of the page.

● Continuing an answer: If you need to use the space to continue an answer, indicate in the original answer space where the answer is continued, i.e. give the page number. Fill in the number of the question that you are continuing to answer at the top of the page.

Working time: 50 minutes.

**Question 1 {1.1.6, 1.1.9} (8 marks)**

Solve the following equations.

1. (1 mark)

|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓ correct solution for  |

1. (2 marks)

|  |
| --- |
|  **Solution** |
|  |
| **Specific behaviours** |
| ✓ eliminates denominators✓ correct solution for  |

1. by using the quadratic formula (2 marks)

|  |
| --- |
|  **Solution** |
|  |
| **Specific behaviours** |
| ✓ uses quadratic formula✓ two solutions for  |

1. by completing the square (3 marks)

|  |
| --- |
|  **Solution** |
|  |
| **Specific behaviours** |
| ✓ completes the square✓ correct values for ✓ two solutions for  |

**Question 2 {1.1.2, 1.1.11} (8 marks)**

1. Point A is the intersection of lines and . Point M (10,18) is the mid-point of Point A and Point B (a, b). Determine the values of a and b. (3 marks)

|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓ determines coordinates for Point A✓ correct value for a✓ correct value for b |

1. A parabola has -axis intercepts ( and and it passes through the point . Find the turning point of this parabola. (2 marks)

|  |
| --- |
| **Solution** |
| Line of symmetry Hence, turning point is  |
| **Specific behaviours** |
| ✓ determines equation in factorised form✓ determines coordinates of turning point |

1. A quadratic function has equation . Find the coordinates of the x-intercepts. (2 marks)

|  |
| --- |
| **Solution** |
| Hence,  |
| **Specific behaviours** |
| ✓ one correct ✓ two correct  |

1. Three quadratic functions , and

. Underneath each function in the table below, write the number of real solution(s). (1 mark)

|  |  |  |  |
| --- | --- | --- | --- |
| Function |  |  |  |
| Number of Solution(s) | 1 | 2 | 0 |

**Question 3 {1.1.22} (6 marks)**

The graph of the relation passes through the points (, 3) and (8,).

1. Determine the values of and .

(3 marks)

|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓ correct value for p✓ one correct value for q✓ two correct values for q |

1. On the axes below, sketch the graph of the relation, labelling all key features with their coordinates or equation.

(3 marks)

|  |
| --- |
| **Solution** |
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|

|  |
| --- |
| **Specific behaviours** |
| ✓ labels vertex (0,1)✓ draws and labels axis of symmetry y=1✓ parabolic shape with smooth curve |

 |
|  |

**Question 4 {1.1.21, 1.1.28} (7 marks)**

Consider the given graph below.

|  |
| --- |
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1. Determine the equations of all the curves forming the shapes in the graph. (5 marks)

|  |
| --- |
| **Solution** |
| Eq1: Eq2: Eq3: Eq4: Eq5:  |
| **Specific behaviours** |
| ✓ correct centre and radius for eq1✓ correct centre and radius for eq2✓ correct centre and radius for eq3✓ correct eq4 **(accept )**✓ correct eq5 **(accept )** |

1. List all the functions in the graph. Justify your answers. (2 marks)

|  |
| --- |
| **Solution** |
| eq4 & eq5. Use the vertical-line test: a vertical line can be drawn that intersects with the graphs of the above equations no more than once, and thus shows two functions. |
| **Specific behaviours** |
| ✓ lists the two functions✓ states vertical-line test |

Question 5 {1.1.16, 1.1.17} (5 marks)

1. Given that for all values of , for suitable values of and . Find and by equating coefficients.

 (2 marks)

|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓ correct value for b✓ correct value for c |

1. Consider the graph of polynomial below. Determine the equation in the form . (3 marks)



|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓ determines coefficient ✓ writes in factorised form✓ writes in general form as required |

**Question 6 {1.1.24, 1.1.25} (6 marks)**

1. State the natural/implied domain and range for each of the relations/functions below.

(3 marks)

|  |  |  |
| --- | --- | --- |
| Relation/Function | Natural Domain | Natural Range |
|  |  |  |
|  |  |  |
|  |  |  |

|  |
| --- |
| **Specific behaviours** |
| ✓ correct natural domain and natural range for ✓ correct natural domain and natural range for ✓ correct natural domain and natural range for  |

1. Sketch the graph of the function, , and state its range. (3 marks)

|  |
| --- |
| **Solution** |
| A close up of a mans face  Description automatically generatedRange is  |
| **1/Specific behaviours** |
| ✓ shape✓ plot or label points or ✓ states the range |

Question 7 {1.4.14} (5 marks)

A and B are independent events. and . Determine

|  |
| --- |
| **Solution** |
| Let Since A and B are independent event Also, Hence,  |
| **Specific behaviours** |
| ✓ states is 0.4✓ uses ✓ uses ✓ forms an equation with ✓ correct number for  |

**Question 8 {1.1.19} (5 marks)**

Let

1. Show that is divisible by . (1 mark)

|  |
| --- |
| **Solution** |
| By the Factor Theorem, is divisible by . |
| **Specific behaviours** |
| ✓ uses the Factor Theorem  |

1. Factorise fully. (4 marks)

|  |
| --- |
| **Solution** |
|          |
| **Specific behaviours** |
| ✓ beginning a division or comparing coefficients✓ finding ✓ finding the correct quotient in full✓ factorising the quotient |

**END OF SECTION ONE**

Additional working space

Question number:

Additional working space

Question number: